SOME REMARKS ON PADAM SINGH'S SAMPLING METHOD

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SUMMARY

Some new results pertaining to Padam Singh's Sampling Method have been derived. Explicit expression of second order inclusion probabilities are derived and some relationships established.

Keywords: Finite population, Inclusion probabilities.

Introduction

In the beginning Padam Singh's sampling method (P. S. Method), is described in brief. Let $U = (U_1, U_2, \ldots, U_N)$ be a finite population of N units and p be a non negative vector (p_1, p_2, \ldots, p_N) such that $\Sigma p_i = 1$. In the sequel for $r > N U_r$ and p_r will mean U_{r-N} and p_{r-N} . P. S. Method is as follows:

(A) Select one unit according to probability vector P. Let the selected unit be U_i , S_i be the subject of U as

$$S_i(U_i, U_{i+1}, U_{i+3}, \ldots, U_{i+2n'-3})$$

where n' = (integral part of N/2) + 1

(B) From S_i select a sample of size n by simple random sampling without replacement (we assume that n < n').

Properties

Here we obtain the first and second order inclusion probabilities namely π_i , π_{ij} and establish a few relations,

Let
$$\delta_i = 1$$
 if *i* is even
= 0 if *i* is odd.

We shall discuss two cases, when N is even and when N is odd separately.

Case No. 1 (When N is even)

It can be easily seen that

$$\pi_i = [\delta_i(1-\alpha) + \alpha(1-\delta_i) + p_i](n/n')$$

Where $\alpha = \sum_{i} \delta_{i} p_{i}$

$$\pi_{ij} = [a_{ij} + b_{ij}][n(n-1)/n'(n'-1)]$$

Where
$$a_{ij} = \delta_i \delta_j (1 - \alpha) + (1 - \delta_i)(1 - \delta_j) \alpha$$

$$b_{ij} = [\delta_i(1-\delta_j) + \delta_j(1-\delta_i)](p_i + p_j)$$

Noting that $\delta_i + 1 = 1 - \delta_i$ and $\delta_{i+2} = \delta_i$

we get the following relationships

$$\pi_{i} + \pi_{i+1} = n(1 + p_{i} + p_{i+1})/n'$$

$$\pi_{i+2} - \pi_{i} = n(p_{i+2} - p_{i})/n'$$
(A)

Case No. II (When N is odd)

It can be easily seen that

$$\pi_{i} = n \left(\sum_{r=0}^{N} \delta_{r} p_{i+r} \right) / n'$$

and for j > i

$$\pi_{ij} = \frac{n(n-1)}{n'(n'-1)} \left[\delta_{j-i} \begin{pmatrix} a \\ \sum_{r=0}^{a} p_{j+2r} \end{pmatrix} + (1 - \delta_{j-i}) \sum_{r=0}^{b} p_{i+2r} \right]$$

where a = [(N-1-j+i)/2], b = [(j-i-1)/2], and

$$[x] = integral part of x.$$

We note the following relationships.

$$\pi_i + \pi_{i+1} = n(1 + p_i)/n'$$

$$\pi_{i+2} - \pi_i = n(p_{i+1} - p_i)/n'$$
(B)

It is interesting to compare (A) and (B).

The use of P. S. Method for inclusion probability proportional to size sampling is discussed by Singh [2] and Deshpande [1].

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REFERENCES

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